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Worldwide Equity Risk Prediction

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Abstract:

Various GARCH models are applied to daily returns of more than 1200 constituents of major stock indices worldwide. The value-at-risk forecast performance is investigated for different markets and industries, considering the test for correct conditional coverage using the false discovery rate (FDR) methodology. For most of the markets and industries we find the same two conclusions. First, an asymmetric GARCH specification is essential when forecasting the 95% value-at-risk. Second, for both the 95% and 99% value-at-risk it is crucial that the innovations' distribution is fat-tailed (e.g., Student- t or – even better – a non-parametric kernel density estimate).

Keywords: GARCH, value-at-risk, equity, worldwide, false discovery rate

JEL Classification: C11, C22, C52

1. Introduction

This note investigates the forecasting performance of commonly used GARCH models over a large universe of worldwide equities. Overall, we consider six markets and eleven industries, for a total of more than twelve hundred time series. We rely on a rolling-window estimation approach and forecast the one-day ahead value-at-risk at the 95% and 99% levels for a total of fifteen years of daily data. To our knowledge, this is the first study which performs such a large-scale forecasting performance exercise. The overall backtest study took three days on a eight-core 2GB machine with computationally efficient parallel C++ implementation. This is of substantial importance for risk-management systems, which need to design suitable risk models for many equities. Obviously, practitioners are typically interested in the risk evaluation of portfolios, where one desires to accurately assess the risk in large multivariate settings. However, this does not make the precise evaluation for one asset irrelevant. For example, the validity of copula models depends not only on the validity of the specification of the dependence structure, but also on the validity of the marginal univariate models. For the models, we rely on symmetric and asymmetric specifications for the variance equation and consider Gaussian, Student- t and kernel-based distributions for the errors. The performance of the different models is compared across markets and industries. Our results indicate that an asymmetric specification is essential when forecasting 95% value-at-risk for equities. For both 95% and 99% value-at-risk it is crucial that the innovations' distribution is fat-tailed. These results are found for most of the markets and industries.

The rest of this note is organized as follows. In section 2 we present the model specifications, the testing and introduce the false discovery rate method. In section 3 we present and discuss the empirical results. Section 4 concludes.

2. Model specification, testing and false discovery rate method

As in [McNeil and Frey \(2000\)](#), each model considered starts with an AR(1) component in order to filter a possible autoregressive part of the equity log-returns. The models differ in the way the volatility of the error terms is modeled. For that purpose, we rely on the symmetric GARCH(1,1) model of [Bollerslev \(1986\)](#) and on the asymmetric GJR(1,1) model by [Glosten et al. \(1993\)](#). The latter accounts for the asymmetric effect of stock return on next period's stock return's variance, known as the leverage effect in the literature ([Black, 1976](#)).

Both models have a long empirical history and have proved to be successful in volatility modeling in several markets ([Bollerslev et al., 1992](#)). They are simple yet powerful GARCH-type models. More specifically, in the GJR model the log-returns r_t are expressed as:

$$\begin{aligned} r_t &= \mu + \rho r_{t-1} + u_t \quad (t = 1, \dots, T) \\ u_t &= \sigma_t \varepsilon_t \quad \varepsilon_t \sim iid f_\varepsilon \\ \sigma_t^2 &= \omega + (\alpha + \gamma 1\{u_{t-1} \leq 0\}) u_{t-1}^2 + \beta \sigma_{t-1}^2, \end{aligned} \tag{1}$$

where $\omega > 0$ and $\alpha, \gamma, \beta \geq 0$ to ensure a positive conditional variance. $1\{\}$ denotes the indicator function, whose value is one if the constraint holds and zero otherwise. No constraints have been imposed to ensure covariance stationarity; however, as a sensitivity analysis we have repeated the whole study with additional covariance stationarity constraints, which yielded approximately the same results with qualitatively equal conclusions. Another sensitivity analysis with the inclusion of 'variance targeting', where the unconditional variance in the GARCH model is set equal to the sample variance – reducing the number of parameters to be estimated by one, led to similar results. The symmetric GARCH model results by imposing $\gamma = 0$. For the distribution f_ε , we consider the simple Gaussian and Student- t distributions, together with a non-parametric Gaussian kernel estimator. The Student- t distribution is probably the most commonly used alternative to the Gaussian for modeling stock returns and allows modeling fatter tails than the Gaussian. The kernel approach gives a non-parametric alternative which can deal with skewness and fat tails in a convenient manner.

Models are fitted by maximum likelihood. For the non-parametric model, the bandwidth is selected by the rule-of-thumb of [Silverman \(1986\)](#) on the residuals of the quasi maximum likelihood fit; alternative bandwidth choices lead to similar results. We rely on the rolling-window approach where 1000 log-returns – i.e., approximately four trading years – are used to estimate the models. Similar results were obtained for windows of 750 and 1500 observations. Then, the next log-return is used as a forecasting window. The model parameters are updated every day. At each time point, the one-day ahead value-at-risk forecast is obtained for the different models. Value-at-risk represents the risk

from market movements as one number: the maximum loss expected on an investment, over a given time period at a specific level of confidence. It is nowadays a standard risk measure of downside risk. In our study, the value-at-risk is a negative percentage; in literature it is sometimes quoted as a positive percentage (i.e., a percentile of the distribution for the negative of the return) or an amount of dollars.

To test the ability of our models to capture the true value-at-risk, we compare the realization of the one-day ahead returns r_{t+1} with the value-at-risk estimates (VaR) at 95% and 99% levels. To that aim, we adopt the backtesting methodology proposed by [Christoffersen \(1998\)](#) which has become the standard practice in financial risk management. This approach is based on the study of the random sequence V_t where $V_t \doteq 1\{r_{t+1} < \text{VaR}_t\}$. A sequence of value-at-risk forecasts at level $(1 - \alpha)$ has correct conditional coverage if the V_t form an independent and identically distributed sequence of Bernoulli random variables with parameter α . In practice, this hypothesis can be verified by testing jointly the independence on the series and the unconditional coverage of the VaR forecasts, i.e., $\mathbb{E}(V_t) = \alpha$. We will estimate the percentage of the time series for which a model provides correct value-at-risk forecasts (in the sense of correct conditional coverage). A naive way to estimate this percentage is to compute the percentage of time series for which the p-value is above a preset significance level, say 5%. However, this approach obviously suffers from Type I errors (rejection for approximately 5% of the time series for which the model performs correctly) and Type II errors (non-rejection for some – or possibly many – of the time series for which the model performs incorrectly). Therefore, the naive estimate may underestimate or overestimate the number of time series for which the model has correct performance, respectively. We therefore correct the percentages of non-rejections using the false discovery rate method of [Storey \(2002\)](#).

Here the key insight of the false discovery rate method is that in case of a model that delivers correct forecasts for a certain time series the p-value is uniformly distributed between zero and one (see, e.g. [Barras et al., 2010](#)). Otherwise, the p-value has an unknown distribution, which should be relatively close to zero. Let λ be the separating value such that for p-values above λ , it is almost certain that they correspond to the null of a correctly performing model. By the properties of the uniform distribution, we can therefore extrapolate the true number of correctly performing models from the p-values exceeding the λ threshold. We rely on the bootstrap method proposed by [Barras et al. \(2010\)](#) to determine the optimal value of λ in a purely data driven way.

3. Results and discussion

We test the performance of the models on constituents of major equity markets worldwide. We consider the regions USA, Western Europe, Asia, South America, Eastern Europe, Middle East and Africa. For each market, all stock constituents of the representative index are considered (using the constituents as of July 2010) for a period ranging from January 1, 1995, to December 31, 2009, thus representing 15 years of daily data. This leads to a database of 3657 equities for which the adjusted daily closing prices are downloaded. The data are then filtered for liquidity following [Lesmond et al. \(1999\)](#). In particular, we remove the time series with less than 1500 data points history, with more than 10% of zero returns and more than two trading weeks of constant price. This filtering approach reduces the database to 1260 time series (around 34% of the overall data set). All data sets are downloaded from Bloomberg. [Tables 1 and 2](#) report a summary of the data used in our analysis. We have chosen this filter, which is obviously rather restrictive since it removes many data series, for the following reasons. First, our aim is a large scale backtest exercise. For this we need a coherent universe of data, where the ‘quality’ of the daily return series should not be too different among regions; this is obtained with the filter. Second, we want to analyze the risk of volatility, not liquidity. Third, the filtered data set represents a universe of stocks where an automated risk management system may be sensible. Nevertheless, we have performed a sensitivity analysis with a different, less stringent filter that led to a smaller reduction of the number of data series; once again, the results were similar.

Forecasting results are reported in [Table 3](#). For most of the markets and industries we find the same two conclusions. First, an asymmetric GARCH specification is essential when forecasting the 95% value-at-risk; the Gaussian GJR model outperforms its symmetric counterpart, the Gaussian GARCH model. On the other hand, when forecasting the 99% value-at-risk the Gaussian GJR model does not outperform the Gaussian GARCH model. Second, for both the 95% and 99% value-at-risk it is crucial that the innovations’ distribution is fat-tailed (e.g., Student- t or a non-parametric kernel density estimate).

Especially for the 99% value-at-risk the performance of the GJR model with kernel density estimate of the innovations’ distribution is remarkable: for the merged population (and most of the markets and industries) the model may

Market	# equities	% total
USA	297	23.6
Western Europe	288	22.8
Asia	477	37.9
South America	90	7.1
Eastern Europe	45	3.6
Africa & Middle East	63	5.0
Total	1260	100

Table 1: Datasets. Number of time series used in the analysis for each market. USA: S&P 500; Western Europe: EuroStoxx 600; Asia: HSCEI (China), HSI (Hong-Kong), KOSPI (South Korea), SENSEX (Bombay), FSSTI (Singapore), TWSE (Taiwan), TPX 100 (Japan); South America: IBOV (Brazil), MEXBOL (Mexico); Eastern Europe: RTSIS\$ (Russia), XU100 (Turkey), WIG (Poland); Middle East and Africa: JALSH (South Africa), HERMES (Egypt), DFMGI (Dubai).

Sector	# equities	% total
Basic Material	144	11.4
Communications	63	5.0
Consumer (cyclical)	144	11.4
Consumer (non-cyclical)	189	15.0
Diversified	9	0.7
Energy	45	3.7
Financial	261	20.7
Funds	36	2.9
Industrial	279	22.1
Technology	63	5.0
Utilities	27	2.1
Total	1260	100

Table 2: Data sets. Number of time series used in the analysis for each sector, as defined by Bloomberg.

yield correct value-at-risk forecasts for the time series of all stock returns. For the 95% value-at-risk the GJR model with kernel is correct for less than 75% of the series. Therefore, an alternative model (e.g., EGARCH, stochastic volatility or regime-switching) or an other estimation method (e.g., Bayesian inference) is required if we desire a correctly performing model for more than 75% of all time series.

We now take a look at the different markets. We see a clear difference between the following two ‘groups’ of regions: (i) USA and Western Europe; (ii) Asia, South America, Eastern Europe, Africa and Middle East. For ‘group’ (i) the GJR model with kernel-based errors is clearly the best model for both 95% and 99% value-at-risk. On the other hand, for ‘group’ (ii) the best model may also be one of the other three models. For Asia and South America the estimated percentage of time series for which the GJR-kernel model provides correct 95% value-at-risk forecasts is lower than the percentage for the GJR model with Gaussian or Student-t errors, respectively. For Eastern Europe, Africa and Middle East the 90% confidence intervals for different models overlap. The GJR-kernel model performs better for (i) than for (ii), arguably because appropriately modeling the properties (i.e., the dynamics and distributions) of stock returns in (ii) is more difficult.

We also consider the different sectors. The GJR model with kernel-based errors performs well for the 99% value-at-risk, except for the ‘Consumer (non-cyclical)’ sector (and ‘Diversified’ but this contains only 9 stocks here). If we compare this model’s prediction quality across the sectors for the 95% value-at-risk, then the worst performance is found for the sectors ‘Consumer (cyclical)’ and ‘Consumer (non-cyclical)’ (except for ‘Diversified’ and ‘Utilities’, where the latter consists of merely 27 stocks). These results suggest that stock returns in the ‘Consumer’ sector(s) have characteristics that are modeled less easily.

For comparison, Tables 4 and 5 show the naive estimation results, the percentage of non-rejections at 5% and 1% significance level, respectively. The relatively low percentage of non-rejections — 93% (96%) in Table 4 (5), as compared with 100% in Table 3 — for the 99% value-at-risk forecasts from the GJR model with kernel-based error distribution (\mathcal{M}_4) is possibly caused by a Type I error for 7% (4%) of the time series. The relatively high percentage of non-rejections — 56% (69%), as compared with 31% in Table 3 — for the 99% value-at-risk forecasts from the GARCH model with Gaussian error distribution (\mathcal{M}_1) is possibly caused by a Type II error for more than 25% (38%) of the time series. Obviously, Type I errors are more harmful in Table 4, whereas Table 5 suffers more from Type II errors.

4. Conclusion

Various GARCH models are fitted to daily returns of more than 1200 constituents of major stock indices worldwide. The value-at-risk forecast performance is investigated for different markets and industries, considering the test for correct conditional coverage using the false discovery rate methodology. For most of the markets and industries we find that an asymmetric GARCH specification is essential when forecasting the 95% value-at-risk. Moreover, for both the 95% and 99% value-at-risk it is crucial that the innovations’ distribution is fat-tailed (e.g., Student- t or – even better – a non-parametric kernel density estimate).

In future research, we intend to consider the performance of Bayesian estimation and alternative model specifications, extending the analysis of Hoogerheide et al. (2012), who only analyze two data series of stock index returns (S&P 500 and Nikkei 225), and using the methods of Hoogerheide et al. (2007) and Hoogerheide and Van Dijk (2010).

References

- Barras, L., Scaillet, O., Wermers, R., 2010. False discoveries in mutual fund performance: Measuring luck in estimated alphas. *Journal of Finance* 65, 179–216.
- Black, F., Jan.–Mar. 1976. The pricing of commodity contracts. *Journal of Financial Economics* 3 (1–2), 167–179.
- Bollerslev, T., Apr. 1986. Generalized autoregressive conditional heteroskedasticity. *Journal of Econometrics* 31 (3), 307–327.
- Bollerslev, T., Chou, R. Y., Kroner, K., Apr.–May 1992. ARCH modeling in finance: A review of the theory and empirical evidence. *Journal of Econometrics* 52 (1–2), 5–59.
- Christoffersen, P. F., Nov. 1998. Evaluating interval forecasts. *International Economic Review* 39 (4), 841–862.
- Glosten, L. R., Jaganathan, R., Runkle, D. E., Dec. 1993. On the relation between the expected value and the volatility of the nominal excess return on stocks. *Journal of Finance* 48 (5), 1779–1801.
- Hoogerheide, L. F., Ardia, D., Corré, N., 2012. Density prediction of stock index returns using GARCH models: Frequentist or Bayesian estimation? *Economics Letters* 116 (3), 322–325.

- Hoogerheide, L. F., Kaashoek, J. F., Van Dijk, H. K., 2007. On the shape of posterior densities and credible sets in instrumental variable regression models with reduced rank: an application of flexible sampling methods using neural networks. *Journal of Econometrics* 139 (1), 154–180.
- Hoogerheide, L. F., Van Dijk, H. K., 2010. Bayesian forecasting of value at risk and expected shortfall using adaptive importance sampling. *International Journal of Forecasting* 26 (2), 231–247.
- Lesmond, D. A., Ogden, Joseph, P., Trzinka, C. A., 1999. A new estimate of transaction costs. *The Review of Financial Studies* 12 (5), 1113–1141.
- McNeil, A. J., Frey, R., Nov. 2000. Estimation of tail-related risk measures for heteroscedastic financial time series: an extreme value approach. *Journal of Empirical Finance* 7 (3–4), 271–300.
- Silverman, B. W., 1986. *Density Estimation for Statistics and Data Analysis*, 1st Edition. Chapman and Hall, New York, USA.
- Storey, J., 2002. A direct approach to false discovery rates. *Journal of the Royal Statistical Society B* 64, 479–498.

	% correct CC95				% correct CC99			
	\mathcal{M}_1	\mathcal{M}_2	\mathcal{M}_3	\mathcal{M}_4	\mathcal{M}_1	\mathcal{M}_2	\mathcal{M}_3	\mathcal{M}_4
Overall	44 [40;48]	56 [53;59]	60 [58;63]	71 [69;74]	31 [27;34]	29 [25;32]	93 [90;95]	100 [98;100]
USA	36 [28;44]	53 [44;63]	68 [63;74]	87 [82;92]	6 [2;9]	7 [3;10]	49 [40;58]	100 [95;100]
Western Europe	29 [22;37]	69 [63;74]	48 [39;57]	78 [72;83]	9 [5;13]	6 [2;9]	90 [85;95]	100 [95;100]
Asia	56 [50;63]	71 [64;78]	55 [51;59]	63 [59;66]	65 [61;69]	49 [42;55]	96 [92;99]	100 [97;100]
South America	16 [1;31]	32 [13;50]	70 [56;85]	26 [8;45]	63 [49;78]	41 [20;61]	82 [67;96]	100 [86;100]
Eastern Europe	44 [6;82]	15 [0;38]	20 [0;51]	50 [23;78]	59 [31;87]	59 [31;87]	100 [74;100]	100 [76;100]
Africa and Middle East	36 [8;64]	36 [8;64]	69 [50;89]	73 [54;93]	31 [7;55]	31 [7;55]	97 [78;100]	45 [14;76]
Basic Material	37 [25;49]	44 [30;57]	50 [36;64]	67 [59;76]	18 [10;27]	22 [12;31]	96 [88;100]	100 [93;100]
Communications	53 [36;70]	52 [43;62]	55 [46;65]	70 [60;80]	41 [26;56]	46 [30;61]	100 [91;100]	100 [92;100]
Consumer (cyclical)	43 [32;54]	61 [48;74]	60 [53;67]	60 [53;67]	27 [18;36]	24 [16;33]	97 [91;100]	100 [94;100]
Consumer (non-cyclical)	13 [7;19]	30 [20;39]	46 [35;58]	62 [55;69]	15 [9;22]	10 [4;15]	49 [37;60]	43 [32;54]
Diversified	14 [0;37]	50 [6;94]	43 [5;80]	57 [15;99]	11 [0;29]	11 [0;29]	64 [38;90]	17 [0;43]
Energy	27 [10;45]	46 [24;68]	53 [40;66]	84 [71;98]	0 [0;0]	0 [0;0]	78 [65;92]	100 [88;100]
Financial	46 [35;58]	67 [60;74]	44 [33;55]	79 [72;86]	29 [19;38]	25 [16;34]	86 [79;93]	100 [94;100]
Funds	28 [8;47]	50 [25;75]	90 [76;100]	90 [76;100]	0 [0;0]	10 [0;20]	100 [86;100]	100 [87;100]
Industrial	47 [38;57]	56 [50;61]	60 [55;66]	74 [68;80]	41 [32;50]	38 [29;46]	99 [94;100]	100 [95;100]
Technology	67 [58;76]	79 [70;88]	75 [66;84]	87 [78;96]	56 [47;65]	60 [51;69]	91 [83;100]	100 [92;100]
Utilities	8 [0;21]	21 [2;40]	57 [25;89]	39 [19;59]	28 [6;50]	21 [2;40]	24 [2;47]	87 [69;100]

Table 3: Estimated percentage of the time series for which the model provides correct value-at-risk forecasts (in the sense of correct conditional coverage) for the 95% (CC95) and 99% (CC99) value-at-risk. Percentages are computed from the individual tests' p-values using the false discovery rate approach of Storey (2002). [·]: asymptotically valid 90% confidence bands derived in Barras et al. (2010). \mathcal{M}_1 : GARCH with Gaussian errors; \mathcal{M}_2 : GJR with Gaussian errors; \mathcal{M}_3 : GJR with Student- t errors; \mathcal{M}_4 : GJR with kernel-based errors.

	% non-rejection CC95				% non-rejection CC99			
	\mathcal{M}_1	\mathcal{M}_2	\mathcal{M}_3	\mathcal{M}_4	\mathcal{M}_1	\mathcal{M}_2	\mathcal{M}_3	\mathcal{M}_4
Overall	57 [55;59]	65 [64;67]	70 [68;71]	77 [76;79]	56 [54;57]	56 [54;58]	88 [87;90]	93 [92;94]
USA	64 [60;67]	73 [69;76]	79 [76;82]	88 [85;90]	36 [32;39]	35 [31;39]	87 [84;89]	92 [90;94]
Western Europe	69 [66;73]	81 [78;84]	76 [73;79]	85 [82;88]	36 [33;40]	36 [33;40]	91 [89;93]	96 [95;98]
Asia	48 [45;51]	54 [51;56]	62 [59;64]	69 [67;72]	74 [72;76]	75 [72;77]	88 [86;90]	92 [90;93]
South America	54 [44;64]	65 [55;75]	73 [64;82]	67 [57;76]	63 [54;73]	65 [55;75]	87 [80;94]	92 [86;98]
Eastern Europe	59 [39;78]	65 [46;84]	71 [52;89]	59 [39;78]	59 [39;78]	65 [46;84]	94 [85;100]	94 [85;100]
Africa and Middle East	68 [55;80]	68 [55;80]	76 [64;87]	78 [67;89]	65 [52;78]	65 [52;78]	95 [88;100]	97 [93;100]
Basic Material	55 [49;61]	60 [55;66]	61 [56;67]	70 [65;76]	62 [57;68]	60 [55;66]	88 [84;92]	95 [92;98]
Communications	53 [46;59]	63 [56;69]	65 [59;72]	81 [76;87]	63 [56;69]	64 [57;71]	95 [92;98]	96 [94;99]
Consumer (cyclical)	53 [48;58]	60 [55;65]	68 [63;72]	73 [68;77]	59 [54;64]	60 [55;65]	91 [88;94]	91 [88;94]
Consumer (non-cyclical)	42 [37;47]	52 [47;57]	66 [61;71]	74 [70;79]	49 [44;54]	51 [46;56]	89 [85;92]	93 [90;95]
Diversified	55 [37;73]	65 [48;82]	65 [48;82]	70 [53;87]	35 [18;52]	40 [22;58]	80 [65;95]	85 [72;98]
Energy	66 [57;75]	82 [75;90]	68 [60;77]	84 [76;91]	29 [20;37]	36 [26;45]	78 [70;86]	93 [88;98]
Financial	66 [62;71]	74 [70;78]	73 [68;77]	82 [78;86]	48 [43;52]	47 [42;52]	88 [84;91]	94 [92;96]
Funds	73 [64;83]	80 [72;88]	92 [86;98]	90 [84;96]	30 [20;40]	25 [16;34]	97 [93;100]	97 [93;100]
Industrial	57 [53;61]	63 [59;67]	71 [68;75]	77 [73;80]	66 [62;70]	66 [62;70]	89 [87;92]	92 [90;94]
Technology	73 [68;79]	81 [76;86]	76 [70;81]	82 [77;87]	61 [55;67]	60 [54;67]	82 [77;87]	91 [88;95]
Utilities	61 [48;73]	73 [62;85]	73 [62;85]	76 [65;87]	46 [34;59]	46 [34;59]	85 [76;94]	90 [83;98]

Table 4: Naive estimation: percentage of non-rejections at the 5% level of the conditional coverage test of [Christoffersen \(1998\)](#) for the 95% (CC95) and 99% (CC99) value-at-risk. []: asymptotically valid 90% confidence bands with naive standard deviation of a proportion. \mathcal{M}_1 : GARCH with Gaussian errors; \mathcal{M}_2 : GJR with Gaussian errors; \mathcal{M}_3 : GJR with Student- t errors; \mathcal{M}_4 : GJR with kernel-based errors.

	% non-rejection CC95				% non-rejection CC99			
	\mathcal{M}_1	\mathcal{M}_2	\mathcal{M}_3	\mathcal{M}_4	\mathcal{M}_1	\mathcal{M}_2	\mathcal{M}_3	\mathcal{M}_4
Overall	72 [70;73]	78 [77;80]	84 [82;85]	90 [89;91]	69 [68;71]	71 [69;72]	94 [93;95]	96 [95;97]
USA	81 [78;84]	87 [84;89]	93 [91;95]	95 [93;96]	53 [50;57]	55 [51;59]	94 [92;96]	98 [96;99]
Western Europe	85 [82;88]	91 [89;94]	91 [89;93]	95 [93;97]	55 [51;59]	56 [52;59]	96 [95;98]	98 [98;99]
Asia	60 [57;62]	67 [64;69]	74 [72;77]	85 [83;87]	83 [81;85]	84 [83;86]	93 [91;94]	94 [92;95]
South America	79 [71;88]	86 [78;93]	95 [91;100]	94 [89;99]	78 [69;86]	83 [75;90]	90 [84;97]	94 [89;99]
Eastern Europe	76 [60;93]	76 [60;93]	82 [67;98]	82 [67;98]	71 [52;89]	76 [60;93]	94 [85;100]	94 [85;100]
Africa and Middle East	81 [71;92]	78 [67;89]	84 [74;94]	89 [81;98]	84 [74;94]	89 [81;98]	97 [93;100]	100 [100;100]
Basic Material	69 [64;75]	72 [67;77]	78 [73;83]	86 [82;90]	75 [70;80]	75 [70;80]	94 [92;97]	97 [95;99]
Communications	71 [64;77]	79 [73;85]	88 [83;92]	91 [87;95]	83 [77;88]	84 [79;89]	98 [96;100]	98 [96;100]
Consumer (cyclical)	65 [61;70]	74 [70;78]	78 [74;83]	89 [86;92]	72 [67;76]	75 [71;79]	94 [91;96]	94 [91;96]
Consumer (non-cyclical)	57 [52;62]	64 [59;69]	78 [73;82]	89 [86;92]	66 [61;71]	66 [62;71]	96 [95;98]	95 [93;97]
Diversified	70 [53;87]	80 [65;95]	85 [72;98]	90 [79;100]	55 [37;73]	50 [32;68]	85 [72;98]	85 [72;98]
Energy	88 [81;94]	93 [88;98]	89 [83;95]	93 [88;98]	48 [38;58]	56 [47;66]	90 [85;96]	97 [94;100]
Financial	82 [78;86]	87 [84;90]	87 [84;90]	93 [90;95]	62 [57;67]	63 [58;67]	92 [89;94]	98 [96;99]
Funds	87 [79;94]	97 [93;100]	97 [93;100]	95 [90;100]	43 [33;54]	47 [36;57]	98 [96;100]	100 [100;100]
Industrial	69 [65;72]	76 [72;79]	83 [80;86]	88 [86;91]	78 [75;81]	77 [74;80]	94 [92;96]	95 [93;97]
Technology	86 [81;90]	89 [85;93]	91 [87;94]	95 [93;98]	66 [60;72]	71 [65;77]	88 [83;92]	96 [94;99]
Utilities	88 [79;96]	88 [79;96]	95 [90;100]	88 [79;96]	61 [48;73]	63 [51;76]	98 [94;100]	95 [90;100]

Table 5: Naive estimation: percentage of non-rejections at the 1% level of the conditional coverage test of [Christoffersen \(1998\)](#) for the 95% (CC95) and 99% (CC99) value-at-risk. []: asymptotically valid 90% confidence bands with naive standard deviation of a proportion. \mathcal{M}_1 : GARCH with Gaussian errors; \mathcal{M}_2 : GJR with Gaussian errors; \mathcal{M}_3 : GJR with Student- t errors; \mathcal{M}_4 : GJR with kernel-based errors.